

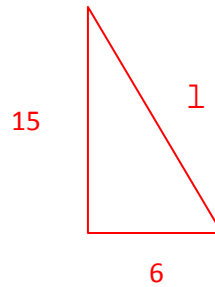
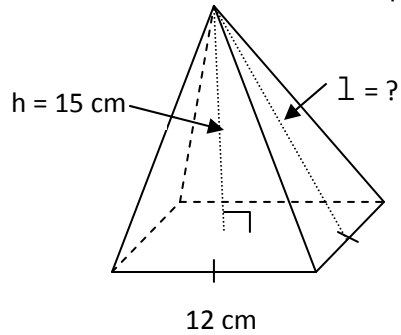
Geometry

Unit: Surface Area and Volume

Section: Surface Area and Volume of Pyramids and Cones

Review Worksheet KEY

1) Find the surface area and volume of the pyramid below.



Find the slant height:

$$6^2 + 15^2 = l^2$$

$$36 + 225 = l^2$$

$$261 = l^2$$

$$16.16 \approx l$$

Find the area of each surface:

Square: $(12)(12) = 144$

Four triangles: $\frac{1}{2}(12)(16.16) = 96.96$

Add the areas together:

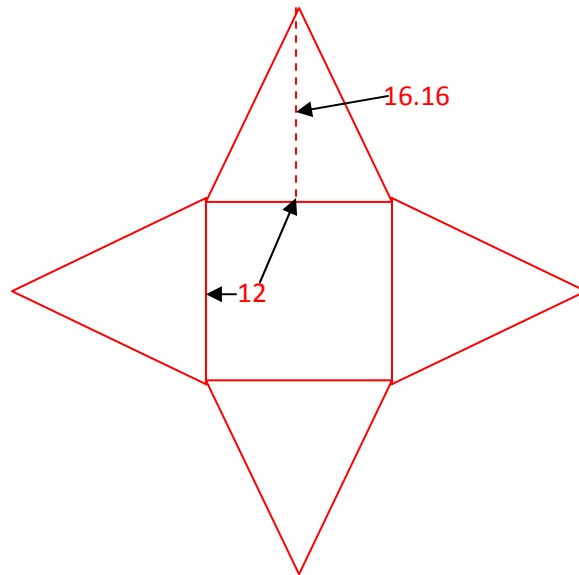
$$144 + 4(96.96) = 531.84$$

Label:

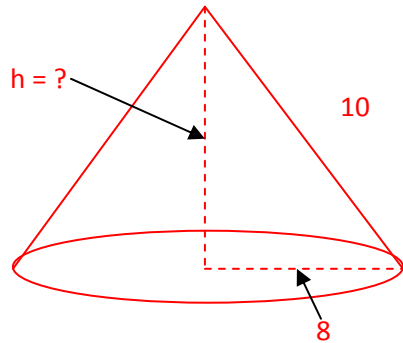
The total surface area is 531.84 cm^2 .

Volume:

$$V = \frac{1}{3}(\text{area of base})(\text{height}) = \frac{1}{3}(144)(15) = 720 \text{ cm}^3.$$



2) Find the surface area and volume of a cone with radius 8 and slant height 10.



$$8^2 + h^2 = 10^2$$

$$64 + h^2 = 100$$

$$h^2 = 36$$

$$h = 6$$

Surface area = $\pi r^2 + \pi r l = \pi(8)^2 + \pi(8)(10) = 144\pi$ units². This is approximately 452.39 units².

$V = \frac{1}{3}(\text{area of base})(\text{height}) = \frac{1}{3}(64\pi)(6) = 128\pi$ units³. This is approximately 402.12 units³.

3) The surface area of a cone is $261\pi \text{ cm}^2$. The radius of the cone is 9 cm. What is the slant height?

What is the height of the cone? What is the volume of the cone?

$$\text{Surface area} = \pi r^2 + \pi r l$$

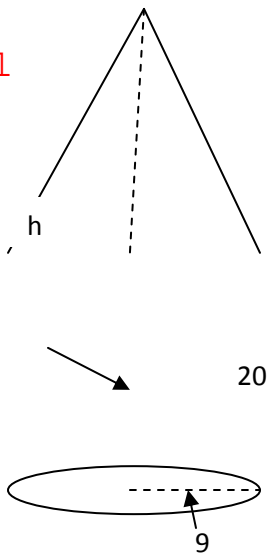
$$261\pi = \pi(9)^2 + \pi(9)l$$

$$261\pi = 81\pi + \pi(9)l$$

$$261\pi = 81\pi + \pi(9)l$$

$$180\pi = 9\pi l$$

$$20 = l$$



$$9^2 + h^2 = 20^2$$

$$81 + h^2 = 400$$

$$h^2 = 319$$

$$h \approx 17.86$$

$$V = \frac{1}{3}(\text{area of base})(\text{height}) = \frac{1}{3}(81\pi)(17.86) \approx 1514.94 \text{ cm}^3.$$